

SHOCKS

MARCH 30, 2009

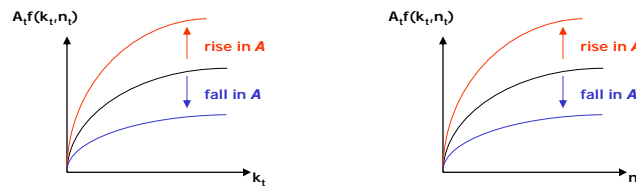
Introduction

BASICS

- ❑ **Shock/shifter**
 - ❑ **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- ❑ Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”

BASICS

- **Shock/shifter**
 - **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”
- Will consider (for now) two types of shocks
 - **Total Factor Productivity (TFP) Shocks** – unexpected changes in A_t in the production function $A_t f(k_t, n_t)$

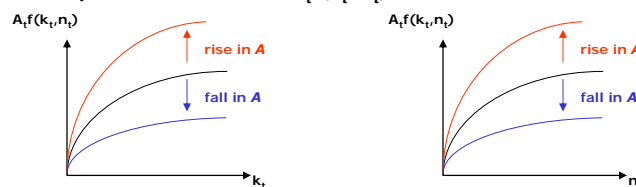


March 30, 2009

3

BASICS

- **Shock/shifter**
 - **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”
- Will consider (for now) two types of shocks
 - **Total Factor Productivity (TFP) Shocks** – unexpected changes in A_t in the production function $A_t f(k_t, n_t)$



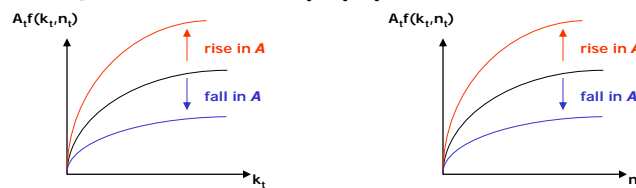
- **Preference Shocks** – unexpected changes in representative consumer’s utility function; causes rotations of indifference maps

March 30, 2009

4

BASICS

- ❑ **Shock/shifter**
 - ❑ **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- ❑ Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”
- ❑ Will consider (for now) two types of shocks
 - ❑ **Total Factor Productivity (TFP) Shocks** – unexpected changes in A_t in the production function $A_t f(k_t, n_t)$



Changes in
“consumer
confidence”

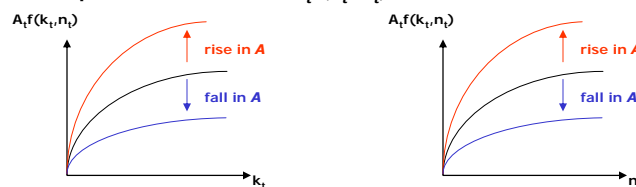
- ❑ **Preference Shocks** – unexpected changes in representative consumer’s utility function; causes rotations of indifference maps

March 30, 2009

5

BASICS

- ❑ **Shock/shifter**
 - ❑ **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- ❑ Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”
- ❑ Will consider (for now) two types of shocks
 - ❑ **Total Factor Productivity (TFP) Shocks** – unexpected changes in A_t in the production function $A_t f(k_t, n_t)$



“SUPPLY
SHOCK”

“DEMAND
SHOCK”

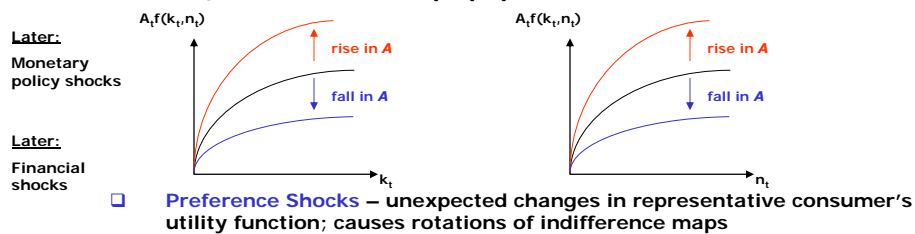
- ❑ **Preference Shocks** – unexpected changes in representative consumer’s utility function; causes rotations of indifference maps

March 30, 2009

6

BASICS

- ❑ **Shock/shifter**
 - ❑ **Definition:** Some unexpected event that affects economic fundamentals and hence decisions, but which is unexplained or unexplainable
- ❑ Introducing shocks into our frameworks (consumption-leisure, consumption-savings, infinite-period) will “get them moving”
- ❑ Will consider (for now) two types of shocks
 - ❑ **Total Factor Productivity (TFP) Shocks** – unexpected changes in A_t in the production function $A_t f(k_t, n_t)$



March 30, 2009

7

TFP IN COBB-DOUGLAS PRODUCTION FUNCTION

- ❑ Revisit the commonly-used functional form in modern quantitative macroeconomic models

$$\text{output}_t = A_t f(k_t, n_t) = A_t k_t^\alpha n_t^{1-\alpha}$$
- ❑ Describes the empirical relationship between aggregate output, aggregate capital, aggregate labor, and **level of sophistication of technology (TFP)**
 - ❑ (How to measure TFP in Chapter 13)
- ❑ Cobb-Douglas form useful for illustrating effects of TFP shocks

March 30, 2009

8

TFP IN COBB-DOUGLAS PRODUCTION FUNCTION

- Revisit the commonly-used functional form in modern quantitative macroeconomic models

$$\text{output}_t = A_t f(k_t, n_t) = A_t k_t^\alpha n_t^{1-\alpha}$$

- Describes the empirical relationship between aggregate output, aggregate capital, aggregate labor, and **level of sophistication of technology (TFP)**

- (How to measure TFP in Chapter 13)

- Cobb-Douglas form useful for illustrating effects of TFP shocks

- Unexpected change (i.e., a shock) in A_t

- Causes change in marginal product of labor

$$mpn_t = \frac{\partial \text{output}_t}{\partial n_t} = A_t f_n(k_t, n_t) = A_t (1-\alpha) k_t^\alpha n_t^{-\alpha}$$

- Causes change in marginal product of capital

$$mpk_t = \frac{\partial \text{output}_t}{\partial k_t} = A_t f_k(k_t, n_t) = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha}$$

March 30, 2009

9

TFP IN COBB-DOUGLAS PRODUCTION FUNCTION

- Revisit the commonly-used functional form in modern quantitative macroeconomic models

$$\text{output}_t = A_t f(k_t, n_t) = A_t k_t^\alpha n_t^{1-\alpha}$$

- Describes the empirical relationship between aggregate output, aggregate capital, aggregate labor, and **level of sophistication of technology (TFP)**

- (How to measure TFP in Chapter 13)

- Cobb-Douglas form useful for illustrating effects of TFP shocks

- Unexpected change (i.e., a shock) in A_t

- Causes change in marginal product of labor

$$mpn_t = \frac{\partial \text{output}_t}{\partial n_t} = A_t f_n(k_t, n_t) = A_t (1-\alpha) k_t^\alpha n_t^{-\alpha}$$

Recall mpn is foundation for labor demand

- Causes change in marginal product of capital

$$mpk_t = \frac{\partial \text{output}_t}{\partial k_t} = A_t f_k(k_t, n_t) = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha}$$

Recall mpk is foundation for capital/investment demand

March 30, 2009

10

TFP SHOCKS AND LABOR DEMAND

- Firm-level demand for labor **defined** by the relation

$$w_t = A_t(1-\alpha)k_t^\alpha n_t^{-\alpha} (= mpn_t)$$

TFP SHOCKS AND LABOR DEMAND

- Firm-level demand for labor **defined** by the relation

$$w_t = A_t(1-\alpha)k_t^\alpha n_t^{-\alpha} (= mpn_t)$$

↓ Because exponent $(-\alpha)$ is a negative number, can move to denominator

$$w_t = A_t(1-\alpha)\left(\frac{k_t}{n_t}\right)^\alpha$$

TFP SHOCKS AND LABOR DEMAND

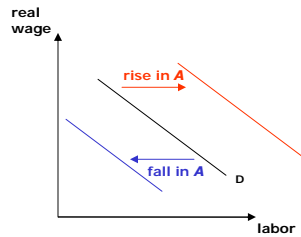
- Firm-level demand for labor **defined** by the relation

$$w_t = A_t(1-\alpha)k_t^\alpha n_t^{-\alpha} (= mpn_t)$$

↓ Because exponent $(-\alpha)$ is a negative number, can move to denominator

$$w_t = A_t(1-\alpha)\left(\frac{k_t}{n_t}\right)^\alpha$$

FOR GIVEN k_t and n_t , rise (fall) in A_t raises (lowers) w_t



March 30, 2009

13

TFP SHOCKS AND LABOR DEMAND

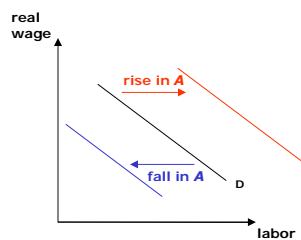
- Firm-level demand for labor **defined** by the relation

$$w_t = A_t(1-\alpha)k_t^\alpha n_t^{-\alpha} (= mpn_t)$$

↓ Because exponent $(-\alpha)$ is a negative number, can move to denominator

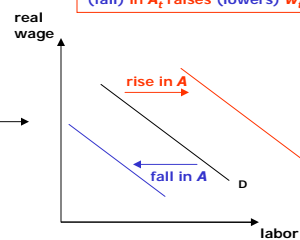
$$w_t = A_t(1-\alpha)\left(\frac{k_t}{n_t}\right)^\alpha$$

FOR GIVEN k_t and n_t , rise (fall) in A_t raises (lowers) w_t



Firm-level labor demand function

Sum over all firms



Aggregate-level labor demand function

- **IMPORTANT:** TFP shocks shift the labor demand curve

March 30, 2009

14

TFP SHOCKS AND CAPITAL DEMAND

- Firm-level demand for capital **defined** by the relation

$$r_t = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha} (= mpk_t)$$

TFP SHOCKS AND CAPITAL DEMAND

- Firm-level demand for capital **defined** by the relation

$$r_t = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha} (= mpk_t)$$

↓ Because exponent $(\alpha - 1)$ is a negative number, can move to denominator

$$r_t = A_t \alpha \left(\frac{n_t}{k_t} \right)^{1-\alpha}$$

TFP SHOCKS AND CAPITAL DEMAND

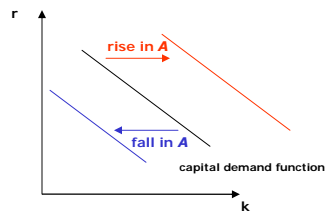
- Firm-level demand for capital **defined** by the relation

$$r_t = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha} (= mpk_t)$$

Because exponent $(\alpha - 1)$ is a negative number, can move to denominator

$$r_t = A_t \alpha \left(\frac{n_t}{k_t} \right)^{1-\alpha}$$

FOR GIVEN k_t and n_t , rise (fall) in A_t raises (lowers) r_t



March 30, 2009

17

TFP SHOCKS AND CAPITAL/INVESTMENT DEMAND

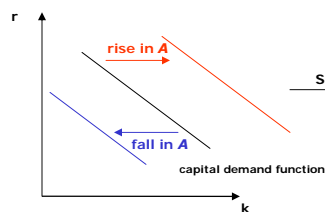
- Firm-level demand for capital **defined** by the relation

$$r_t = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha} (= mpk_t)$$

Because exponent $(\alpha - 1)$ is a negative number, can move to denominator

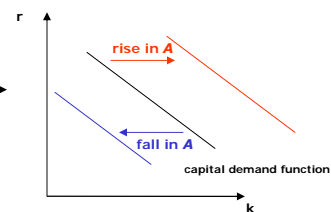
$$r_t = A_t \alpha \left(\frac{n_t}{k_t} \right)^{1-\alpha}$$

FOR GIVEN k_t and n_t , rise (fall) in A_t raises (lowers) r_t



Firm-level capital demand function

Sum over all firms



Aggregate-level capital demand function

- **IMPORTANT:** TFP shocks shift the capital demand (and hence investment demand – recall $inv_t = k_{t+1} - k_t$) curve

March 30, 2009

18

PREFERENCE SHOCKS

- Illustrate idea using consumption-leisure model
 - Preference shocks in consumption-savings model: Practice Problem Set 5
- Utility function (modified from Chapter 2): $u(Bc, l)$
 - c : consumption
 - l : leisure
 - B : preference shifter, with $B > 0$
 - Chapter 2: were implicitly considering $B = 1$

PREFERENCE SHOCKS

- Illustrate idea using consumption-leisure model
 - Preference shocks in consumption-savings model: Practice Problem Set 5
- Utility function (modified from Chapter 2): $u(Bc, l)$
 - c : consumption
 - l : leisure
 - B : preference shifter, with $B > 0$
 - Chapter 2: were implicitly considering $B = 1$
- Mechanics of B
 - Makes *each* unit of c more (high B) desirable...
 - ...or less (low B) desirable

PREFERENCE SHOCKS

- ❑ Illustrate idea using consumption-leisure model
 - ❑ Preference shocks in consumption-savings model: Practice Problem Set 5
 - ❑ Utility function (modified from Chapter 2): $u(Bc, l)$
 - ❑ c : consumption
 - ❑ l : leisure
 - ❑ B : preference shifter, with $B > 0$
 - ❑ Chapter 2: were implicitly considering $B = 1$
 - ❑ Mechanics of B
 - ❑ Makes each unit of c more (high B) desirable...
 - ❑ ...or less (low B) desirable
 - ❑ Interpretation of B
 - ❑ "Cultural" events that alter individuals' desires
 - ❑ "Political" events that alter individuals' desires
 - ❑ Any other events that alter individuals' desires
- } Society-wide events that alter a given person's desires – hence "taken as given" by an individual

PREFERENCE SHOCKS

- ❑ Illustrate idea using consumption-leisure model
 - ❑ Preference shocks in consumption-savings model: Practice Problem Set 5
 - ❑ Utility function (modified from Chapter 2): $u(Bc, l)$
 - ❑ c : consumption
 - ❑ l : leisure
 - ❑ B : preference shifter, with $B > 0$
 - ❑ Chapter 2: were implicitly considering $B = 1$
 - ❑ Mechanics of B
 - ❑ Makes each unit of c more (high B) desirable...
 - ❑ ...or less (low B) desirable
 - ❑ Interpretation of B
 - ❑ "Cultural" events that alter individuals' desires
 - ❑ "Political" events that alter individuals' desires
 - ❑ Any other events that alter individuals' desires
- } Society-wide events that alter a given person's desires – hence "taken as given" by an individual
- ↑ Could interpret as the foundation of "consumer confidence"

PREFERENCE SHOCKS

- MRS between consumption and leisure

- Definition is same as always

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$

PREFERENCE SHOCKS

- MRS between consumption and leisure

- Definition is same as always

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$

- But now need chain rule of calculus to compute $\partial u / \partial c$

- Because first argument of $u(\cdot)$ is now the composite Bc , not simply c

PREFERENCE SHOCKS

- MRS between consumption and leisure
 - Definition is same as always

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$
 - But now need chain rule of calculus to compute $\partial u / \partial c$
 - Because first argument of $u(\cdot)$ is now the **composite** Bc , not simply c
- Chain rule: $\partial u / \partial c = u_1(Bc, l) \cdot B$ (grab the **B** term inside the first argument)

March 30, 2009

25

PREFERENCE SHOCKS

- MRS between consumption and leisure
 - Definition is same as always

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$
 - But now need chain rule of calculus to compute $\partial u / \partial c$
 - Because first argument of $u(\cdot)$ is now the **composite** Bc , not simply c
- Chain rule: $\partial u / \partial c = u_1(Bc, l) \cdot B$ (grab the **B** term inside the first argument)
- MU of leisure same as always: $\partial u / \partial l = u_2(Bc, l)$
- → MRS between consumption and leisure
 - **B** affects MRS in "two" ways

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{1}{B} \cdot \frac{u_2(Bc, l)}{u_1(Bc, l)}$$

March 30, 2009

26

PREFERENCE SHOCKS

- MRS between consumption and leisure
 - Definition is same as always

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$
 - But now need chain rule of calculus to compute $\partial u / \partial c$
 - Because first argument of $u(\cdot)$ is now the **composite** Bc , not simply c
 - Chain rule: $\partial u / \partial c = u_1(Bc, l) \cdot B$ (grab the **B** term inside the first argument)
 - MU of leisure same as always: $\partial u / \partial l = u_2(Bc, l)$
 - → MRS between consumption and leisure
 - **B** affects MRS in “two” ways

The effects of **B** here affect indifference curves

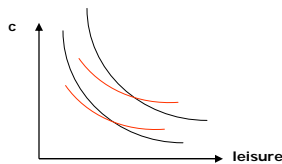
$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{1}{B} \cdot \frac{u_2(Bc, l)}{u_1(Bc, l)}$$

The effects of **B** here cancel out (affects numerator and denominator in same way)

PREFERENCE SHOCKS AND INDIFFERENCE MAPS

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{1}{B} \cdot \frac{u_2(Bc, l)}{u_1(Bc, l)}$$

IF B RISES



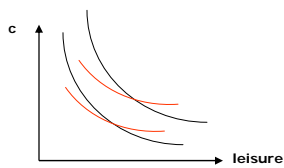
Rise in **B** flattens all indifference curves (i.e., lowers **MRS** at any point in c - l space).

Interpretation: each unit of c more valuable, so **decreased willingness** to trade c for one more unit of l

PREFERENCE SHOCKS AND INDIFFERENCE MAPS

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{1}{B} \cdot \frac{u_2(Bc,l)}{u_1(Bc,l)}$$

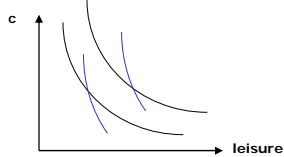
IF B RISES



Rise in **B** flattens all indifference curves (i.e., lowers **MRS** at any point in **c-l** space).

Interpretation: each unit of **c** more valuable, so **decreased willingness** to trade **c** for one more unit of **l**

IF B FALLS



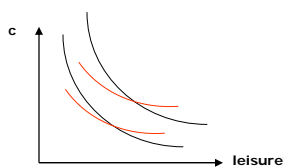
Fall in **B** steepens all indifference curves (i.e., raises **MRS** at any point in **c-l** space).

Interpretation: each unit of **c** less valuable, so **increased willingness** to trade **c** for one more unit of **l**

PREFERENCE SHOCKS AND INDIFFERENCE MAPS

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{1}{B} \cdot \frac{u_2(Bc,l)}{u_1(Bc,l)}$$

IF B RISES

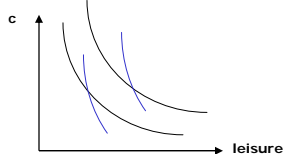


Rise in **B** flattens all indifference curves (i.e., lowers **MRS** at any point in **c-l** space).

Interpretation: each unit of **c** more valuable, so **decreased willingness** to trade **c** for one more unit of **l**

Superimpose a budget line:
optimal choice of **c** and **l**
clearly affected by shock to **B**

IF B FALLS

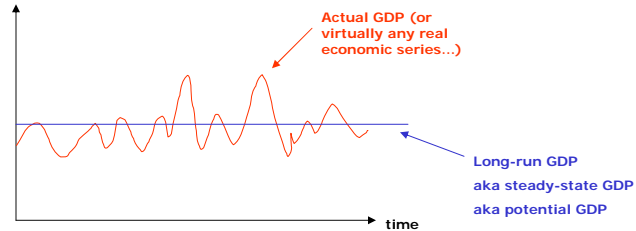


Fall in **B** steepens all indifference curves (i.e., raises **MRS** at any point in **c-l** space).

Interpretation: each unit of **c** less valuable, so **increased willingness** to trade **c** for one more unit of **l**

PREVIEW OF BUSINESS CYCLE THEORY

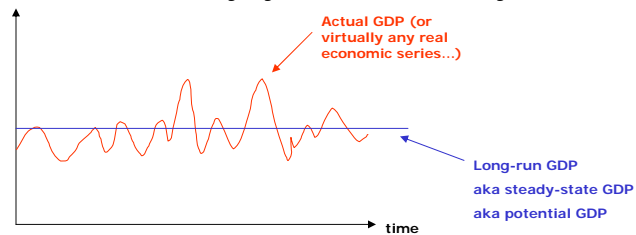
- ❑ Modern macro view: periodic ups and downs of macroeconomic activity driven fundamentally by (various and many) shocks



- ❑ Supply shocks: TFP shocks, others
- ❑ Demand shocks: preference shocks, monetary policy shocks (Chapter 14), others

PREVIEW OF BUSINESS CYCLE THEORY

- ❑ Modern macro view: periodic ups and downs of macroeconomic activity driven fundamentally by (various and many) shocks



- ❑ Supply shocks: TFP shocks, others
- ❑ Demand shocks: preference shocks, monetary policy shocks (Chapter 14), others

- ❑ Shocks over time lead to changes over time in
 - ❑ Consumers' incentives to work, save, and consume
 - ❑ Firms' incentives to hire, invest, and produce
- Economy's response(s) to shocks mediated through labor markets, capital markets, and goods markets

INTERTEMPORAL CONSUMPTION- LEISURE FRAMEWORK

MARCH 30, 2009

Introduction

BASICS

- **Consumption-Leisure Framework**
 - Foundation for goods-market demand and labor-market supply
 - Optimality condition
$$\frac{\partial u / \partial l}{\partial u / \partial c} = (1-t)w$$
- **Consumption-Savings Framework**
 - Foundation for (period- t) goods-market demand and asset-market supply
 - Optimality condition
$$\frac{\partial u / \partial c_1}{\partial u / \partial c_2} = 1+r$$

BASICS

- ❑ Consumption-Leisure Framework
 - ❑ Foundation for goods-market demand and labor-market supply
 - ❑ Optimality condition

$$\frac{\partial u / \partial l}{\partial u / \partial c} = (1-t)w$$
- ❑ Consumption-Savings Framework
 - ❑ Foundation for (period- t) goods-market demand and asset-market supply
 - ❑ Optimality condition

$$\frac{\partial u / \partial c_1}{\partial u / \partial c_2} = 1+r$$
- ❑ Bring together consumption-savings margin with the consumption-leisure margin
- ❑ Utility function: $v(c_1, l_1, c_2, l_2) = u(c_1, l_1) + u(c_2, l_2)$
 - ❑ Dropping the assumption from simple (Chapter 3 and 4) two-period framework that income “falls from the sky”
 - ❑ Representative consumer has to work for his (labor) income in each period

Can put a β here

UTILITY AND BUDGET CONSTRAINTS

- ❑ Utility function: $v(c_1, l_1, c_2, l_2) = u(c_1, l_1) + u(c_2, l_2)$
- ❑ Budget constraints
 - ❑ Period-1 budget constraint (nominal terms)

$$P_1 c_1 + A_1 - A_0 = iA_0 + (1-t_1)W_1(168-l_1)$$
 - ❑ Period-2 budget constraint (nominal terms)

$$P_2 c_2 + A_2 - A_1 = iA_1 + (1-t_2)W_2(168-l_2)$$

UTILITY AND BUDGET CONSTRAINTS

- Utility function: $v(c_1, l_1, c_2, l_2) = u(c_1, l_1) + u(c_2, l_2)$
- Budget constraints
 - Period-1 budget constraint (nominal terms)

$$P_1 c_1 + A_1 - A_0 = iA_0 + (1-t_1)W_1(168-l_1)$$
 - Period-2 budget constraint (nominal terms)

$$P_2 c_2 + A_2 - A_1 = iA_1 + (1-t_2)W_2(168-l_2)$$
- Derive (nominal) LBC as usual (solve P2BC for A_1 and insert in P1BC)

$$P_1 c_1 + \frac{P_2 c_2}{1+i} = (1-t_1)W_1(168-l_1) + \frac{(1-t_2)W_2(168-l_2)}{1+i} + (1+i)A_0$$

UTILITY AND BUDGET CONSTRAINTS

- Utility function: $v(c_1, l_1, c_2, l_2) = u(c_1, l_1) + u(c_2, l_2)$
- Budget constraints
 - Period-1 budget constraint (nominal terms)

$$P_1 c_1 + A_1 - A_0 = iA_0 + (1-t_1)W_1(168-l_1)$$
 - Period-2 budget constraint (nominal terms)

$$P_2 c_2 + A_2 - A_1 = iA_1 + (1-t_2)W_2(168-l_2)$$
- Derive (nominal) LBC as usual (solve P2BC for A_1 and insert in P1BC)

$$P_1 c_1 + \frac{P_2 c_2}{1+i} = (1-t_1)W_1(168-l_1) + \frac{(1-t_2)W_2(168-l_2)}{1+i} + (1+i)A_0$$
- Or in real terms (work out details yourself)

$$c_1 + \frac{c_2}{1+r} = (1-t_1)w_1(168-l_1) + \frac{(1-t_2)w_2(168-l_2)}{1+r} + (1+r)a_0$$

UTILITY AND BUDGET CONSTRAINTS

- Utility function: $v(c_1, l_1, c_2, l_2) = u(c_1, l_1) + u(c_2, l_2)$
- Budget constraints
 - Period-1 budget constraint (nominal terms)

$$P_1 c_1 + A_1 - A_0 = iA_0 + (1-t_1)W_1(168-l_1)$$
 - Period-2 budget constraint (nominal terms)

$$P_2 c_2 + A_2 - A_1 = iA_1 + (1-t_2)W_2(168-l_2)$$
- Derive (nominal) LBC as usual (solve P2BC for A_1 and insert in P1BC)

$$P_1 c_1 + \frac{P_2 c_2}{1+i} = (1-t_1)W_1(168-l_1) + \frac{(1-t_2)W_2(168-l_2)}{1+i} + (1+i)A_0$$
- Or in real terms (work out details yourself)

$$c_1 + \frac{c_2}{1+r} = (1-t_1)w_1(168-l_1) + \frac{(1-t_2)w_2(168-l_2)}{1+r} + (1+r)a_0$$
- Or if infinite number of periods

$$\sum_{t=0}^{\infty} \frac{c_t}{(1+r)^t} = \sum_{t=0}^{\infty} \frac{(1-t_t)w_t(168-l_t)}{(1+r)^t} + (1+r)a_0$$
 - Assuming r is constant every period (slightly more complicated expression if r_t varies every period)

March 30, 2009

39

CONSUMPTION-SAVINGS MARGIN

- Describes decision of how much to consume "today" (period t) versus save for "tomorrow" (period $t+1$)
 - A decision that spans periods
- Think of as orthogonal to (i.e., independent of) the consumption-leisure margin
- Optimal choice (two-period model) described by

$$\frac{\partial u / \partial c_1}{\partial u / \partial c_2} = 1 + r$$

March 30, 2009

40

CONSUMPTION-SAVINGS MARGIN

- Describes decision of how much to consume “today” (period t) versus save for “tomorrow” (period $t+1$)
 - A decision that spans periods
- Think of as orthogonal to (i.e., independent of) the consumption-leisure margin
- Optimal choice (two-period model) described by

$$\frac{\partial u / \partial c_1}{\partial u / \partial c_2} = 1 + r$$

- Optimal choice (infinite-period model) described by

$$\frac{\partial u / \partial c_t}{\partial u / \partial c_{t+1}} = 1 + r_t$$

CONSUMPTION-SAVINGS MARGIN

- Describes decision of how much to consume “today” (period t) versus save for “tomorrow” (period $t+1$)
 - A decision that spans periods
- Think of as orthogonal to (i.e., independent of) the consumption-leisure margin
- Optimal choice (two-period model) described by

$$\frac{\partial u / \partial c_1}{\partial u / \partial c_2} = 1 + r$$

- Optimal choice (infinite-period model) described by

$$\frac{\partial u / \partial c_t}{\partial u / \partial c_{t+1}} = 1 + r_t, \quad \frac{\partial u / \partial c_{t+1}}{\partial u / \partial c_{t+2}} = 1 + r_{t+1}, \quad \frac{\partial u / \partial c_{t+2}}{\partial u / \partial c_{t+3}} = 1 + r_{t+2}, \quad \frac{\partial u / \partial c_{t+4}}{\partial u / \partial c_{t+5}} = 1 + r_{t+4}, \quad \text{etc.}$$

- Recall: can think of infinite-period model as sequence of overlapping two-period models

CONSUMPTION-LEISURE MARGIN

- ❑ Describes decision **within a period** of how much to consume versus how much to enjoy leisure
 - ❑ A decision that does **not** span periods
- ❑ Think of as orthogonal to (i.e., independent of) the consumption-savings margin
- ❑ Optimal choice (two-period model) described by

$$\frac{\partial u / \partial l_1}{\partial u / \partial c_1} = (1-t_1)w_1 \qquad \frac{\partial u / \partial l_2}{\partial u / \partial c_2} = (1-t_2)w_2 \qquad \text{i.e., for each of the two periods}$$

CONSUMPTION-LEISURE MARGIN

- ❑ Describes decision **within a period** of how much to consume versus how much to enjoy leisure
 - ❑ A decision that does **not** span periods
- ❑ Think of as orthogonal to (i.e., independent of) the consumption-savings margin
- ❑ Optimal choice (two-period model) described by

$$\frac{\partial u / \partial l_1}{\partial u / \partial c_1} = (1-t_1)w_1 \qquad \frac{\partial u / \partial l_2}{\partial u / \partial c_2} = (1-t_2)w_2 \qquad \text{i.e., for each of the two periods}$$

- ❑ Optimal choice (infinite-period model) described by

$$\frac{\partial u / \partial l_t}{\partial u / \partial c_t} = (1-t_t)w_t, \quad \frac{\partial u / \partial l_{t+1}}{\partial u / \partial c_{t+1}} = (1-t_{t+1})w_{t+1}, \quad \frac{\partial u / \partial l_{t+2}}{\partial u / \partial c_{t+2}} = (1-t_{t+2})w_{t+2}, \quad \text{etc.}$$

- ❑ Consumption-leisure decision "looks the same every period" in infinite-period environment

BUILDING BLOCKS OF MODERN MACRO THEORY

- ❑ Intertemporal consumption-leisure model is the foundation of almost all modern conceptual macroeconomic frameworks
 - ❑ Referred to as **Dynamic General Equilibrium (DGE) Models**
 - ❑ Both Real Business Cycle (RBC) models and New Keynesian (NK) models (the two dominant current schools of macroeconomic thinking)

BUILDING BLOCKS OF MODERN MACRO THEORY

- ❑ Intertemporal consumption-leisure model is the foundation of almost all modern conceptual macroeconomic frameworks
 - ❑ Referred to as **Dynamic General Equilibrium (DGE) Models**
 - ❑ Both Real Business Cycle (RBC) models and New Keynesian (NK) models (the two dominant current schools of macroeconomic thinking)
- ❑ Power of DGE models demonstrated by RBC theorists in early 1980's – idea of DGE models has been adopted by nearly all other macro camps
 - ❑ Even though important ideological differences between NK Theory and RBC Theory
 - ❑ **DGE methodology has been universally adopted**

BUILDING BLOCKS OF MODERN MACRO THEORY

- ❑ Intertemporal consumption-leisure model is the foundation of almost all modern conceptual macroeconomic frameworks
 - ❑ Referred to as **Dynamic General Equilibrium (DGE) Models**
 - ❑ Both Real Business Cycle (RBC) models and New Keynesian (NK) models (the two dominant current schools of macroeconomic thinking)

- ❑ Power of DGE models demonstrated by RBC theorists in early 1980's – idea of DGE models has been adopted by nearly all other macro camps
 - ❑ Even though important ideological differences between NK Theory and RBC Theory
 - ❑ **DGE methodology has been universally adopted**

- ❑ Three seminal phases of the history of macroeconomic thought/practice
 - ❑ Measuring macroeconomic activity (1930's – 1950)
 - ❑ Keynesian-inspired macroeconometric models (1950 – 1970's)
 - ❑ DGE methodology (1980's – today)