

THE FINANCIAL ACCELERATOR: FINANCIAL MARKETS AND THE MACROECONOMY

APRIL 20, 2009

Introduction

FINANCIAL ACCELERATOR

- ❑ **“Financial accelerator” framework**
 - ❑ The most widely-used and applied framework in macroeconomic theory and policy for thinking about financial markets
 - ❑ Developed in series of studies by Bernanke, Gertler, and Gilchrist in late 1980’s and early 1990’s
- ❑ **Popular-press language**
 - ❑ “Financial accelerator”
 - ❑ “Financial feedback loops”
 - ❑ “Loan spirals”
- ❑ **Describes well many of the financial-macroeconomic linkages underpinning the dynamics of**
 - ❑ **The Great Depression**
 - ❑ **Current macroeconomic conditions**

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 - ❑ The Great Depression
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- ❑ **Will develop idea in context of firm theory (Chapter 6)**
- ❑ Can also develop idea in context of consumer theory (Chapter 3, Chapter 4, Chapter 8)
 - ❑ Recall “credit constraint” analysis of consumption/savings decisions (Problem Set 4)

OUTLINE OF FRAMEWORK

Major ideas underlying Financial Accelerator Framework

1. Firms’ **financial** assets (i.e., stocks and bonds) matter for their ability to purchase **physical** assets (i.e., machines and equipment)
2. Market **prices** of financial assets matter for **firm financing constraints**
3. Government regulation affects the linkage between financial markets and real (i.e., goods and physical capital) markets through financing constraints

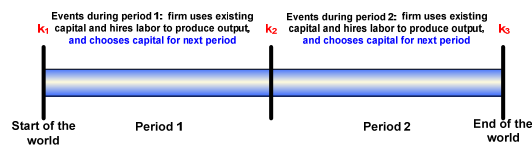
OUTLINE OF FRAMEWORK

Four Building Blocks of the Financial Accelerator Framework

1. **Two-Period Model of Firms**
 - Based on Chapter 6
 - Enriched to allow for both **physical** assets (machines and equipment) and **financial** assets (stocks and bonds)
2. **Financing Constraint**
 - Quantity of **physical** capital firms can purchase depends on the market value of their **financial** assets
 - Reflects market and regulatory structures designed to mitigate **informational asymmetries**
 - (Recall basic Chapter 6 theory of firms featured no constraints on firm profit maximization)
3. **Government Regulation/Oversight of Financial Relationships**
4. **Relationship between Firm Profits and Dividends**

BASIC FIRM THEORY

□ Timeline of events

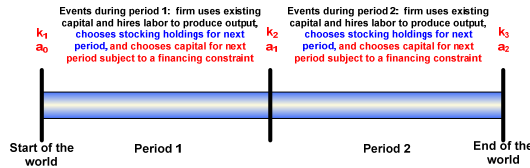


□ Notation

- k_1 : capital used for production in period 1 (decided upon in "period 0")
- n_1 : labor used for production in period 1
- w_1 : real wage rate for labor in period 1 ($w_1 = W_1/P_1$)
- i : nominal interest rate (between period 1 and period 2)
- P_1 : nominal price of output produced and sold by firm in period 1 AND nominal price of one unit of capital bought by the firm in period 1 for use in period 2

ENRICHING THE BASIC FIRM THEORY

Timeline of events



Notation

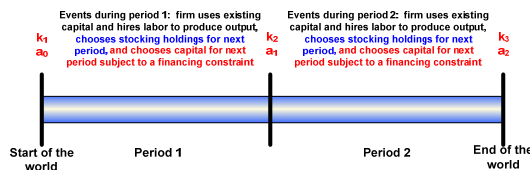
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 - a_0 : real wealth (stock) holdings at beginning of period 1/end of period 0
 - S_1 : nominal price of a unit of stock in period 1
 - D_1 : nominal dividend paid in period 1 by each unit of stock held at the start of period 1
- The "defining features" of stock

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ENRICHING THE BASIC FIRM THEORY

Timeline of events



Notation

- k_2 : capital used for production in period 2 (decided upon in period 1)
 - n_2 : labor used for production in period 2
 - w_2 : real wage rate for labor in period 2 ($w_2 = W_2/P_2$)
 - i : nominal interest rate (between period 1 and period 2)
 - P_2 : nominal price of output produced and sold by firm in period 2 AND nominal price of one unit of capital bought by the firm in period 2 for use in period 3
 - a_1 : real wealth (stock) holdings at beginning of period 2/end of period 1
 - S_2 : nominal price of a unit of stock in period 2
 - D_2 : nominal dividend paid in period 2 by each unit of stock held at the start of period 2
 - π_2 : net inflation rate between period 1 and period 2 (recall: $\pi_2 = P_2/P_1 - 1$)
- The "defining features" of stock

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RATES OF RETURN

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REAL INTEREST RATE ON GOVERNMENT BONDS: A "SAFE" ASSET
 - Thus can think of bonds (one type of financial asset) as being in the background of the analysis
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REAL INTEREST RATE ON STOCKS: A "RISKY" ASSET
 - Measures the net dollar return (in period 2) on one share of stock (whose purchase price was S_1 in period 1)
- Can distinguish two measures of **real** interest rates in this framework

FIRM PROFIT FUNCTION

- A **dynamic** profit maximization problem
 - Because firm exists for both periods
 - All analysis conducted from the perspective of the very beginning of period 1
 - → Must consider present-discounted-value (PDV) of lifetime (i.e., two-period) profits

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- **Dynamic profit function**
 - (specified in nominal terms – could specify in real terms...)

Period-1 profits

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1$$

Total revenue
in period 1
(price x
output)

Value of
pre-existing
physical
capital (an
asset for
firms)

Total labor
cost in
period 1

Total cost of
buying
physical
capital for
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(time to build
→ must
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Total cost of buying financial assets (i.e., stock-holdings in other firms) for period 2

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Period-1 profits (PDV of) period-2 profits

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

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$$\underbrace{P_1 f(k_1, n_1)}_{\text{Total revenue in period 1}} + \underbrace{P_1 k_1}_{\text{Value of pre-existing physical capital}} + \underbrace{(S_1 + D_1)a_0}_{\text{Value (inclusive of dividends) of pre-existing financial assets}} - \underbrace{P_1 w_1 n_1}_{\text{Total labor cost in period 1}} - \underbrace{P_1 k_2}_{\text{Total cost of buying physical capital for period 2}} - \underbrace{S_1 a_1}_{\text{Total cost of buying financial assets}} + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2)a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

(PDV of) period-2 profits = 0 = 0

As usual: no physical or financial assets needed for "period 3"

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Total cost of buying financial assets (i.e., stock-holdings in other firms) for period 2

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INFORMATIONAL ASYMMETRIES

- "Informational asymmetries" pervasive in borrowing/lending relationships
- Borrower (whether consumer or firm) **much** more likely to know his own ability/willingness to repay a loan
 - Lenders often have very little information about the "quality" or "trustworthiness" of a borrower
 - An asymmetry of information

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 - ❑ **On consumer side**
 - ❑ e.g., down payment on house purchase
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} If you stop making your house or car payments, you lose the down payment (in addition to the car or house...), which might make individual think twice **before** borrowing

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- ❑ **Note:** the basic informational asymmetry **itself** cannot be mitigated...

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FINANCING CONSTRAINT

- ❑ Capture this idea through a **financing constraint** on firm's ability to purchase capital between period 1 and period 2
- ❑ **Financing constraint**
 - ❑ **Total expenditures on period-1 physical investment must be equal to market value of firm's financial (stock) holdings**
 - ❑ (Technically, smaller than or equal to, so an inequality constraint...but will only analyze constraint with equality)

$$P_1 \cdot inv_1 = S_1 \cdot a_1$$

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- **Important: a_1 appears in the financing constraint, not a_0**
 - Idea this assumption captures: firm might try to strategically manipulate the value of *financial* assets it holds in order to affect the quantity of *physical* investment it can engage in
 - (From the perspective of beginning of period 1, a_1 has not yet been chosen, whereas a_0 is pre-determined)

GOVERNMENT OVERSIGHT OF FINANCIAL MARKETS

- **Government oversight of informational asymmetries in borrower/lender relationships**
 - **Filing of proper documentation**
 - **Full disclosure (“truth-in-lending”) laws**
 - **Direct lending in some markets**
 - ...

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- **Capture government Regulation of financial dealings in our framework in very simple way**
 - **Firm can only borrow up to a fraction R of the market value of its financial assets for physical investment purposes**
 - **e.g., if government mandates that expenditures on physical investment can only comprise 80% of market value of financial assets, $R = 0.80$**

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Impose this financing constraint on firm profit maximization problem

FINANCIAL ACCELERATOR FRAMEWORK

□ Four Building Blocks of the Financial Accelerator Framework

1. Firm Profit Function

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

= 0 = 0

2. Financing Constraint

$$P_1 \cdot (k_2 - k_1) = S_1 \cdot a_1$$

3. Government Regulation of Financial Relationships (imposition of **R** on financing constraint)

$$P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$$

4. Relationship between firm profits and dividends

COMING SOON

FIRM PROFIT MAXIMIZATION

Maximize two-period profits

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

= 0 = 0

Subject to financing constraint

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Subject to financing constraint

$$P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$$

Construct Lagrangian

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} + \lambda [R \cdot S_1 \cdot a_1 - P_1 \cdot (k_2 - k_1)]$$

Lagrange multiplier on financing constraint

FIRM PROFIT MAXIMIZATION

Maximize two-period profits

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

Subject to financing constraint

$$P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$$

Construct Lagrangian

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} + \lambda [R \cdot S_1 \cdot a_1 - P_1 \cdot (k_2 - k_1)]$$

Lagrange multiplier on financing constraint

CRUCIAL OBSERVATION: in basic firm theory (i.e., Chapter 6), value of this multiplier was....

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Lagrange multiplier on financing constraint

CRUCIAL OBSERVATION: in basic firm theory (i.e., Chapter 6), value of this multiplier was....

$\lambda = 0$ i.e., there was no financing constraint!

KEY QUESTION: What regulatory and/or market features make the financing constraint effectively "disappear" (i.e., cause $\lambda = 0$)?

FIRM PROFIT MAXIMIZATION

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□ FOCs with respect to n_1, n_2

□ FOCs with respect to k_2, a_1

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□ **FOCs with respect to n_1, n_2**

Identical except for time subscripts

→ with respect to n_1 : $\cancel{P_1} f_n(k_1, n_1) - \cancel{P_1} w_1 = 0$ Equation 1

→ with respect to n_2 : $\frac{\cancel{P_2} f_n(k_2, n_2)}{1+i} - \frac{\cancel{P_2} w_2}{1+i} = 0$ Equation 2

- Financing constraint does not affect profit-maximizing choices of labor hiring...
- ...thus same analysis from Chapter 6 of labor demand curve, etc, applies

□ **FOCs with respect to k_2, a_1**

FIRM PROFIT MAXIMIZATION

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□ **FOCs with respect to k_2, a_1**

- The interesting aspects of this framework
- **The heart of the accelerator mechanism**

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with respect to k_2 :

with respect to a_1 :

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□ **FOCs with respect to k_2, a_1**

with respect to k_2 : $-P_1 + \frac{P_2 f_k(k_2, n_2)}{1+i} + \frac{P_2}{1+i} - \lambda P_1 = 0$ Equation 3

with respect to a_1 : $-S_1 + \frac{S_2 + D_2}{1+i} + \lambda \cdot R \cdot S_1 = 0$ Equation 4

□ **Analysis of Equation 4 in isolation**

- **Answers the central question: under what conditions does $\lambda = 0$?**
- Reveals how stock market returns affect financing constraints
- Reveals how government regulation affects financing constraints

□ **Analysis of Equation 3 and Equation 4 jointly**

- **Demonstrates how/why financial market prices (i.e., stock prices/returns) matter for macroeconomic activity**
- **The financial accelerator effect**

WHY IS FINANCING A *CONSTRAINT*?

$$-S_1 + \frac{S_2 + D_2}{1+i} + \lambda \cdot R \cdot S_1 = 0 \quad \text{Equation 4}$$

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↓ Solve for λ

$$\lambda = \left[S_1 - \frac{S_2 + D_2}{1+i} \right] \cdot \frac{1}{R \cdot S_1}$$

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↓ Use definition of inflation, $1 + \pi_2 = P_2 / P_1$, and regroup terms

$$\lambda = \left[1 - \frac{S_2 + D_2}{S_1} \cdot \frac{P_1}{P_2} \cdot \frac{1 + \pi_2}{1+i} \right] \cdot \frac{1}{R}$$

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↓ Use definition of "nominal interest rate on stock", $1 + i^{STOCK} = (S_2 + D_2) / S_1$
Use definition of inflation, $1 + \pi_2 = P_2 / P_1$

$$\lambda = \left[1 - \frac{1 + i^{STOCK}}{1 + \pi_2} \cdot \frac{1 + \pi_2}{1+i} \right] \cdot \frac{1}{R}$$

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Use definition of "nominal interest rate on stock", $1 + r^{STOCK} = (S_2 + D_2) / S_1$
 Use definition of inflation, $1 + \pi_2 = P_2 / P_1$

$$\lambda = \left[1 - \frac{1 + i^{STOCK}}{1 + \pi_2} \cdot \frac{1 + \pi_2}{1 + i} \right] \cdot \frac{1}{R}$$

Fisher equation for stock: $1 + r^{STOCK} = (1 + \beta^{STOCK}) / (1 + n_2)$
 Fisher equation for bonds: $1 + r = (1 + i) / (1 + n_2)$

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Final rewrite!

$$\lambda = \left[\frac{r - r^{STOCK}}{1 + r} \right] \cdot \frac{1}{R} \quad \text{The Lagrange multiplier on firm's financing constraint}$$

WHY IS FINANCING A CONSTRAINT?

$$\lambda = \left[\frac{r - r^{STOCK}}{1 + r} \right] \cdot \frac{1}{R} \quad \text{The Lagrange multiplier on firm's financing constraint}$$

- Basic firm theory (Chapter 6)
 - No financing constraint

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- Basic firm theory (Chapter 6)
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 - Can interpret basic firm theory analysis as featuring $\lambda = 0$
 - Interpretation: under "normal market conditions," financing constraints don't matter (much...)

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} + \lambda [R \cdot S_1 \cdot a_1 - P_1 \cdot (k_2 - k_1)] = 0$$

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- **If $\lambda = 0$ (i.e., "normal market conditions")**
 - **Labor demand decisions unaffected by financial market conditions**
 - **Capital demand decisions unaffected by financial market conditions**
- **Key question: what causes $\lambda = 0$?**

WHY IS FINANCING A CONSTRAINT?

$$\lambda = \left[\frac{r - r^{STOCK}}{1 + r} \right] \cdot \frac{1}{R} \quad \text{The Lagrange multiplier on firm's financing constraint}$$

- **Two conditions for $\lambda = 0$**
 - **Market returns on risky assets equal returns on safe assets**
 - **Risky assets: stocks**
 - **Safe assets**
 - **Bonds (financial)**

WHY IS FINANCING A CONSTRAINT?

$$\lambda = \left[\frac{r - r^{STOCK}}{1 + r} \right] \cdot \frac{1}{R}$$

The Lagrange multiplier on firm's financing constraint

Two conditions for $\lambda = 0$

- Can think of both government bonds (financial assets) and machines & equipment (physical assets) as "safe": you (pretty much...) know what you're going to get from them.
- Market returns on risky assets equal returns on safe assets
 - Risky assets: stocks
 - Safe assets
 - Bonds (financial)
 - Machines and equipment (physical) – most directly relevant for firms' production and sales activity!
 - Basic firm theory prediction: $r = mpk$

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$$r = r^{STOCK} \longrightarrow \lambda = 0$$

Interpretation: if returns on financial assets match up with returns on physical assets, financing constraints "don't matter"

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 - The larger is R , the lower is λ

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 - The larger is R , the lower is λ
 - Financing constraint: $P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$
 - Market value of financial assets
 - Market value of financial assets, higher R allows higher k_2

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Holding constant market value of financial assets, higher R allows higher k_2

$$R = \infty \longrightarrow \lambda = 0$$

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Financing constraint: $P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$

Holding constant market value of financial assets, higher R allows higher k_2

In practice, not literally infinity...

$$R = \infty \longrightarrow \lambda = 0$$

Interpretation: if government regulations allow high borrowing with little assets, financing constraints "don't matter"

FINANCING CONSTRAINT AND CAPITAL DEMAND

- Assume $R = 1$ under "normal conditions" (but keep R in rest of analysis)
 - $R > 1$ is "lax regulation" (because it lowers λ , all else constant)
 - $R < 1$ is "tight regulation" (because it increases λ , all else constant)
 - → Whether or not financing constraint matters (i.e., whether or not $\lambda = 0$) all depends on whether or not $r^{STOCK} = r$ or not

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$$-P_1 + \frac{P_2 f_k(k_2, n_2)}{1+i} + \frac{P_2}{1+i} - \lambda P_1 = 0 \quad \text{Equation 3 (FOC on } k_2)$$

$$\lambda = \left[\frac{r - r^{STOCK}}{1+r} \right] \cdot \frac{1}{R} \quad \text{Equation 4 (FOC on } a_1)$$

- Basic firm theory (Chapter 6)
 - Capital demand function derived from Equation 3
 - Idea still the same...but now complicated by the financing constraint

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↓ Substitute λ from Equation 4 into Equation 3

$$-P_1 + \frac{P_2 f_k(k_2, n_2)}{1+i} + \frac{P_2}{1+i} - \left[\frac{r - r^{STOCK}}{1+r} \right] \frac{1}{R} P_1 = 0$$

↓ Rearrange

FINANCING CONSTRAINT AND CAPITAL DEMAND

$$-P_1 + \frac{P_2 f_k(k_2, n_2)}{1+i} + \frac{P_2}{1+i} - \left[\frac{r - r^{STOCK}}{1+r} \right] \frac{1}{R} P_1 = 0 \quad (\text{from previous page})$$

↓ Divide by P_1

$$\frac{P_2 f_k(k_2, n_2)}{P_1(1+i)} + \frac{P_2}{P_1(1+i)} - \left[\frac{r - r^{STOCK}}{1+r} \right] \frac{1}{R} = 1$$

FINANCING CONSTRAINT AND CAPITAL DEMAND

$$-P_1 + \frac{P_2 f_k(k_2, n_2)}{1+i} + \frac{P_2}{1+i} - \left[\frac{r - r^{STOCK}}{1+r} \right] \frac{1}{R} P_1 = 0 \quad (\text{from previous page})$$

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↓ Use definition of inflation, $1 + \pi_2 = P_2 / P_1$

$$\left(\frac{1 + \pi_2}{1+i} \right) f_k(k_2, n_2) + \frac{1 + \pi_2}{1+i} - \left[\frac{r - r^{STOCK}}{1+r} \right] \frac{1}{R} = 1$$

FINANCING CONSTRAINT AND CAPITAL DEMAND

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↓ Divide by P_1

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↓ Use definition of inflation, $1 + n_2 = P_2 / P_1$

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FINANCING CONSTRAINT AND CAPITAL DEMAND

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Multiply by $(1+r)$

Marginal product of capital, mpk

$$f_k(k_2, n_2) + 1 - \frac{r - r^{STOCK}}{R} = 1 + r$$

Assuming $R = 1$ under "normal conditions," but keeping R in the analysis

COBB-DOUGLAS PRODUCTION FUNCTION

- A commonly-used functional form in modern quantitative macroeconomic models

$$f(k, n) = k^\alpha n^{1-\alpha}$$
- Describes the empirical relationship between aggregate GDP, aggregate capital, and aggregate labor quite well
- $\alpha \in (0, 1)$ measures **capital's share of output**
 - Hence $(1-\alpha) \in (0, 1)$ measures **labor's share of output**
 - **Interpretation**
 - The relative importance of (either) capital (or labor) in the production process
 - **Estimates for U.S. economy:** $\alpha \approx 0.3$
 - **Estimates for Chinese economy:** $\alpha \approx 0.15$ (not (yet) a very capital-rich economy)
- **Cobb-Douglas form useful for illustrating factor demands**
 - $mpn = f_n(k, n) = (1-\alpha)k^\alpha n^{-\alpha}$
 - $mpk = f_k(k, n) = \alpha k^{\alpha-1} n^{1-\alpha}$

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FINANCING CONSTRAINT AND CAPITAL DEMAND

- Firm-level demand for capital **defined** by the relation

$$r = \alpha k^{\alpha-1} n^{1-\alpha} - \left[\frac{r - r^{STOCK}}{R} \right] \left(= mpk - \left[\frac{r - r^{STOCK}}{R} \right] \right)$$

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$$\left[1 + \frac{1}{R} \right] r = \alpha k^{\alpha-1} n^{1-\alpha} + \frac{r^{STOCK}}{R}$$

$$\left[\frac{R+1}{R} \right] r = \alpha k^{\alpha-1} n^{1-\alpha} + \frac{r^{STOCK}}{R}$$

$$r = \left(\frac{R}{R+1} \right) \alpha k^{\alpha-1} n^{1-\alpha} + \frac{r^{STOCK}}{R+1}$$

Solve for r (return on "safe" physical assets)

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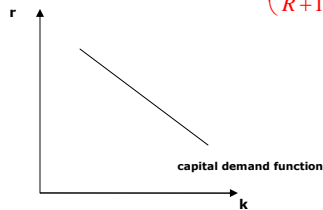
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CHAPTER 6: NEGATIVE RELATIONSHIP BETWEEN r AND k



FINANCING CONSTRAINT AND CAPITAL DEMAND

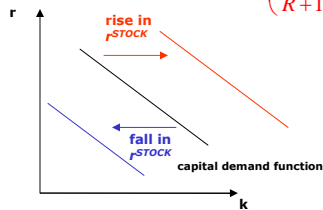
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Rise (fall) in return on stock leads to shift out (in) of capital demand function



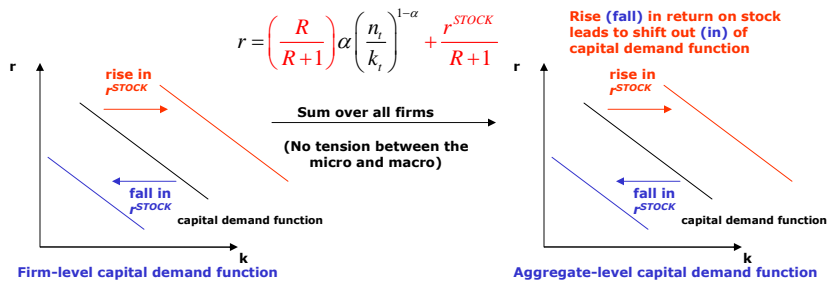
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- **IMPORTANT:** changes in financial market returns shift capital demand (and hence investment demand – recall $inv_t = k_{t+1} - k_t$)

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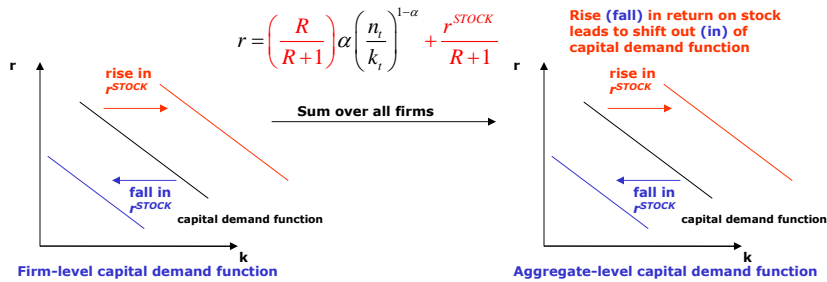
FINANCING CONSTRAINT AND CAPITAL DEMAND

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- Next: the financial accelerator
- Next: the role of financial oversight

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FINANCIAL ACCELERATOR FRAMEWORK

□ **Four Building Blocks of the Financial Accelerator Framework**

1. Firm Profit Function

$$P_1 f(k_1, n_1) + P_1 k_1 + (S_1 + D_1) a_0 - P_1 w_1 n_1 - P_1 k_2 - S_1 a_1 + \frac{P_2 f(k_2, n_2)}{1+i} + \frac{P_2 k_2}{1+i} + \frac{(S_2 + D_2) a_1}{1+i} - \frac{P_2 w_2 n_2}{1+i} - \frac{P_2 k_3}{1+i} - \frac{S_2 a_2}{1+i}$$

= 0 = 0

2. Financing Constraint

$$P_1 \cdot (k_2 - k_1) = S_1 \cdot a_1$$

3. Government Regulation of Financial Relationships (imposition of R on financing constraint)

$$P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$$

4. Relationship between firm profits and dividends

NOW

DIVIDENDS AND PROFITS

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 - Some industries' dividend policies subject to government regulation
 - Recently: financial companies receiving government funding have had dividend payments limited to \$0.01 per share
- **Recent average: ≈ 35 percent of profits disbursed as dividends**
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$$D_t = P_t \cdot \text{profit}_t \quad \leftarrow \text{REAL profits of firm in period } t$$

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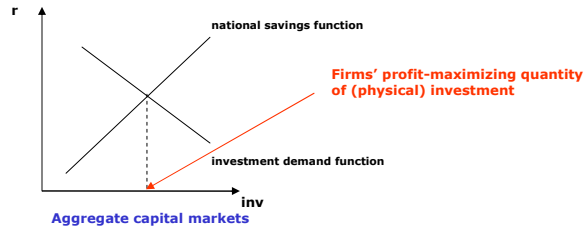
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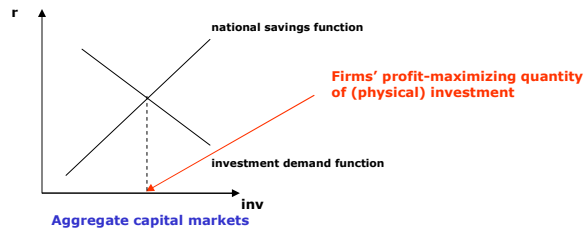
FINANCIAL ACCELERATOR IN ACTION

- Suppose economy is in a “steady-state” in which $r = r^{STOCK}...$



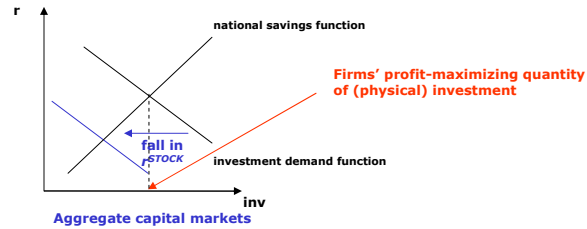
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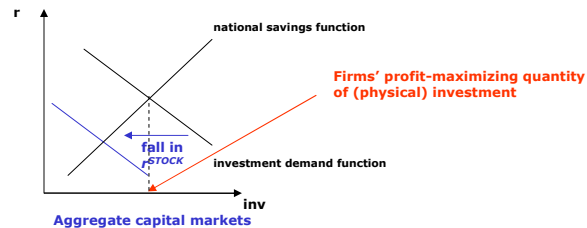


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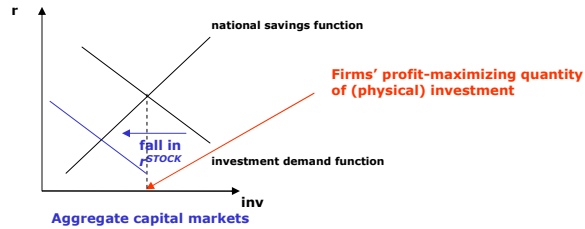
- **Equilibrium quantity of (physical) investment falls**
 - Investment \approx 15% of GDP

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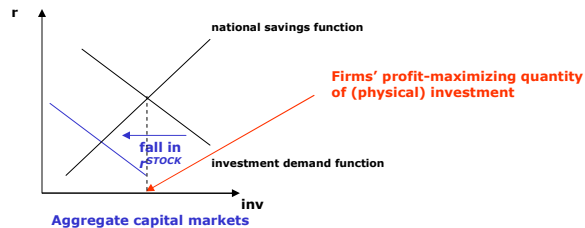
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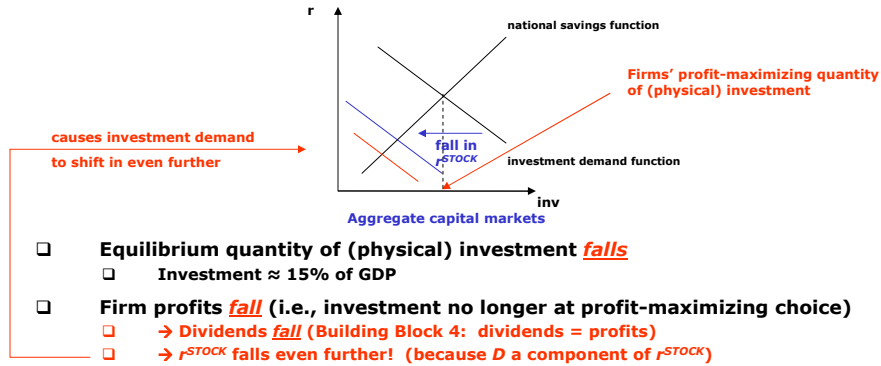
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 - $\rightarrow r^{STOCK}$ falls even further! (because D a component of r^{STOCK})

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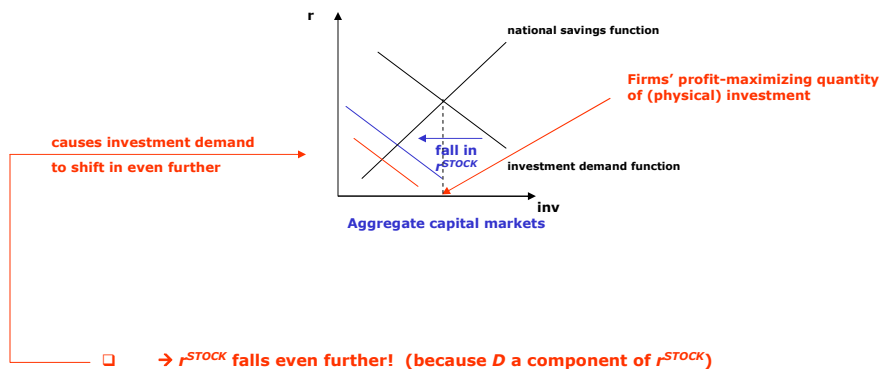


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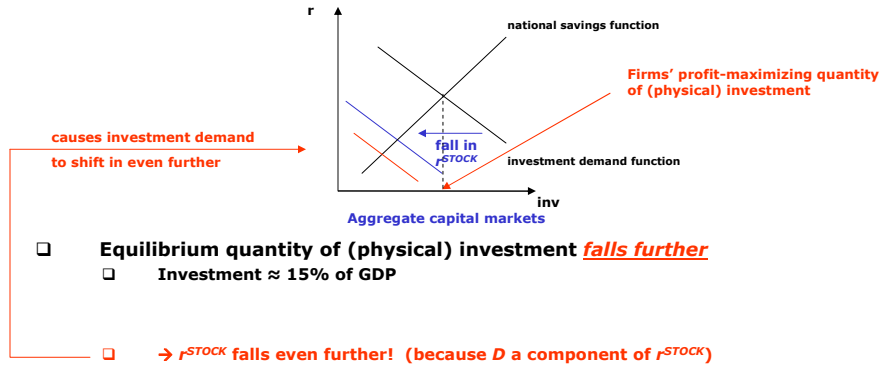


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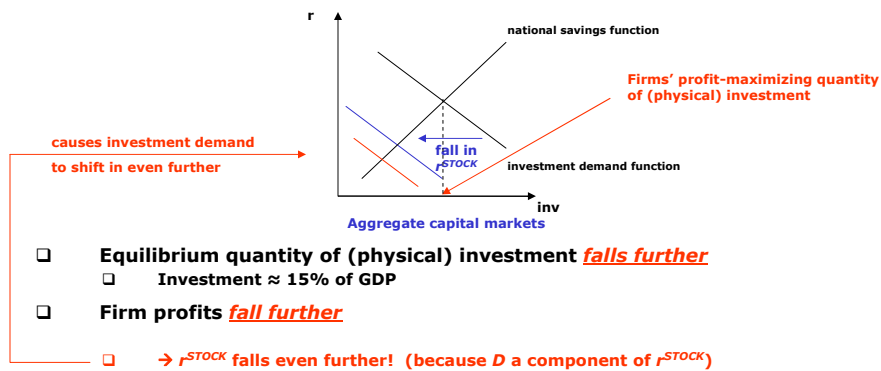


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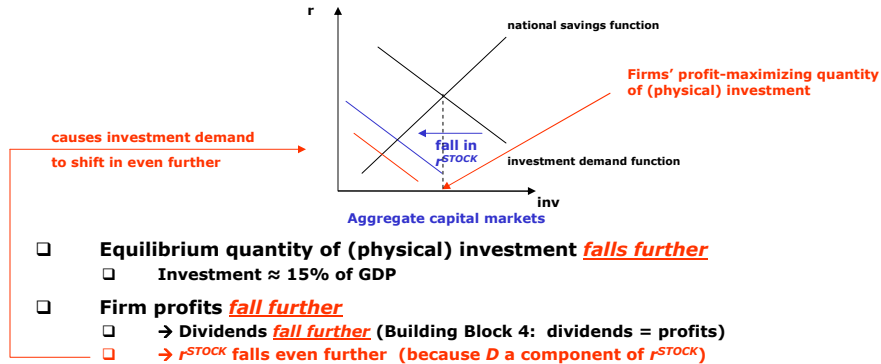


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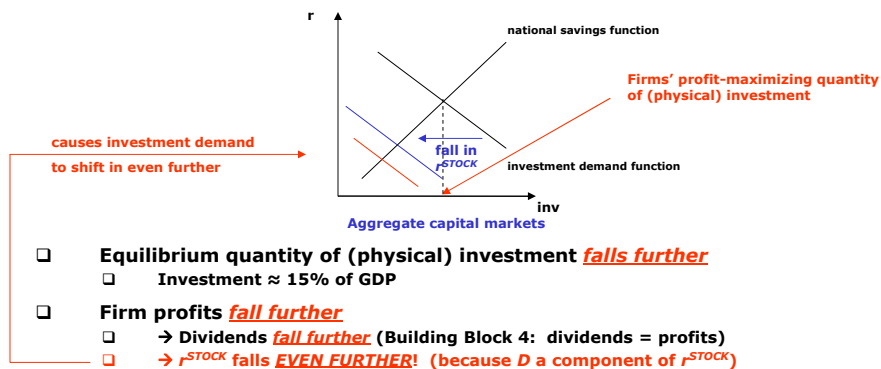


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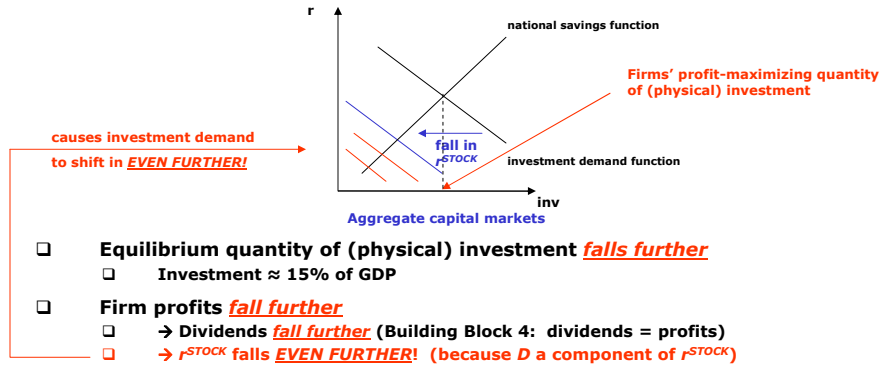


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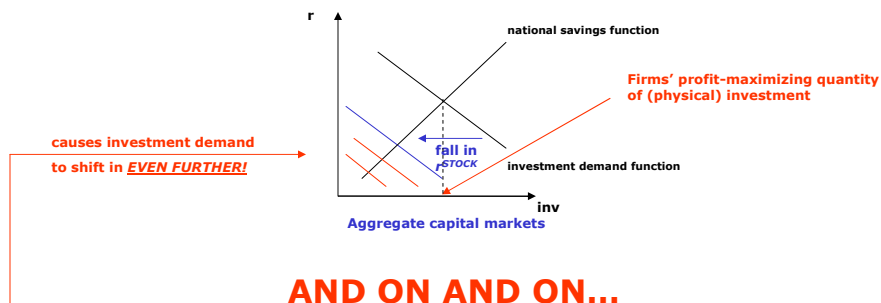


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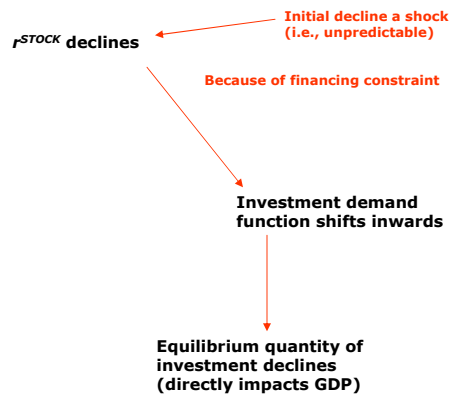
FINANCIAL ACCELERATOR

r_{STOCK} declines ← Initial decline a shock (i.e., unpredictable)

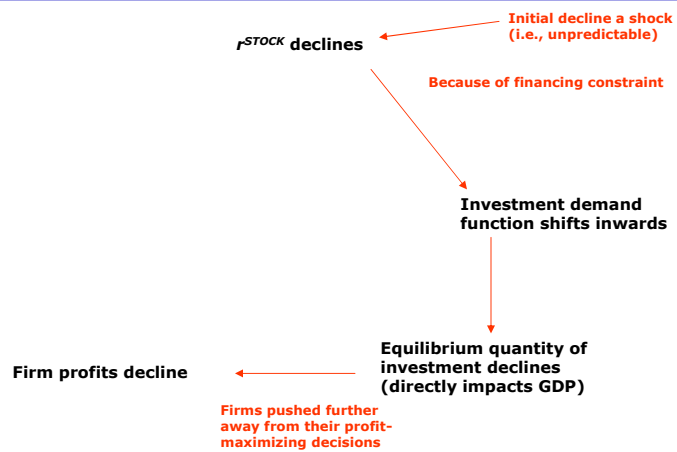
FINANCIAL ACCELERATOR

r_{STOCK} declines ← Initial decline a shock (i.e., unpredictable)
Because of financing constraint
Investment demand function shifts inwards

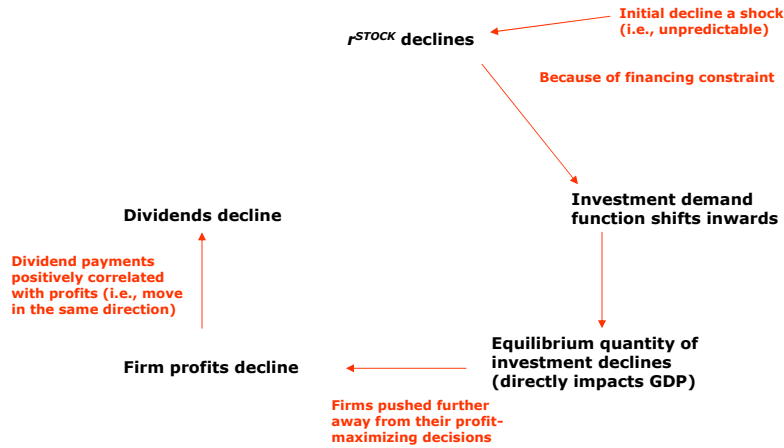
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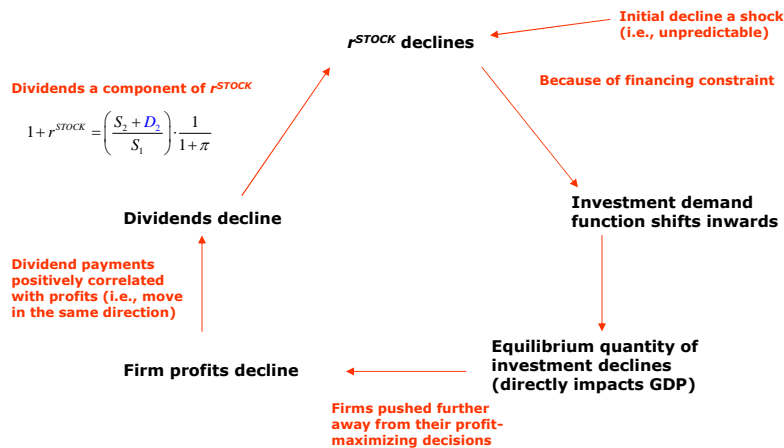
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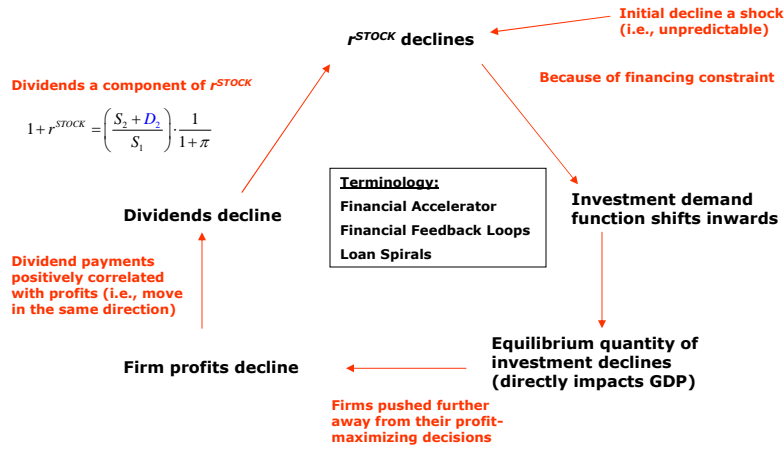
FINANCIAL ACCELERATOR



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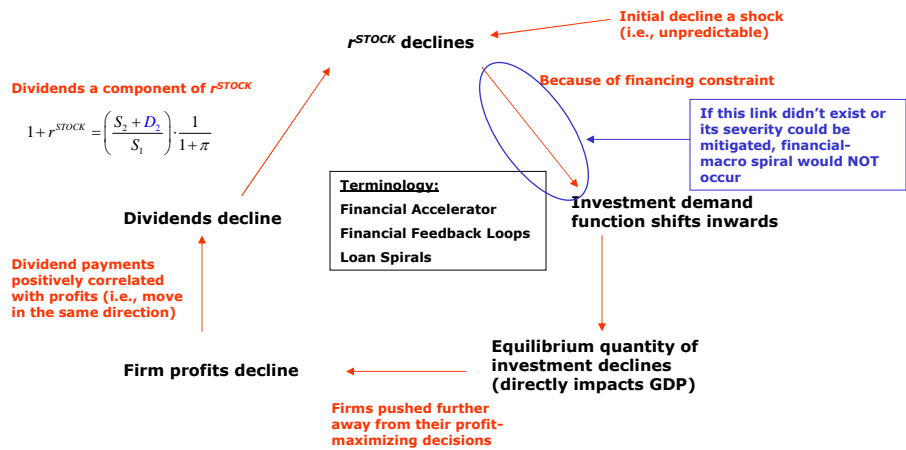
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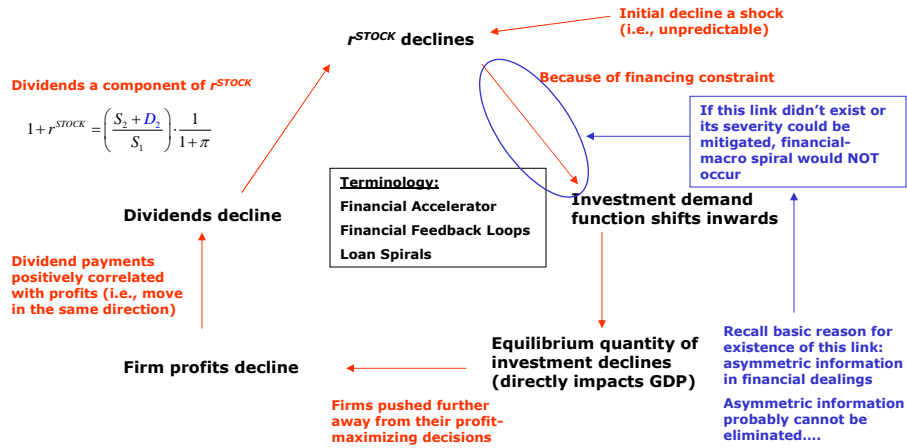
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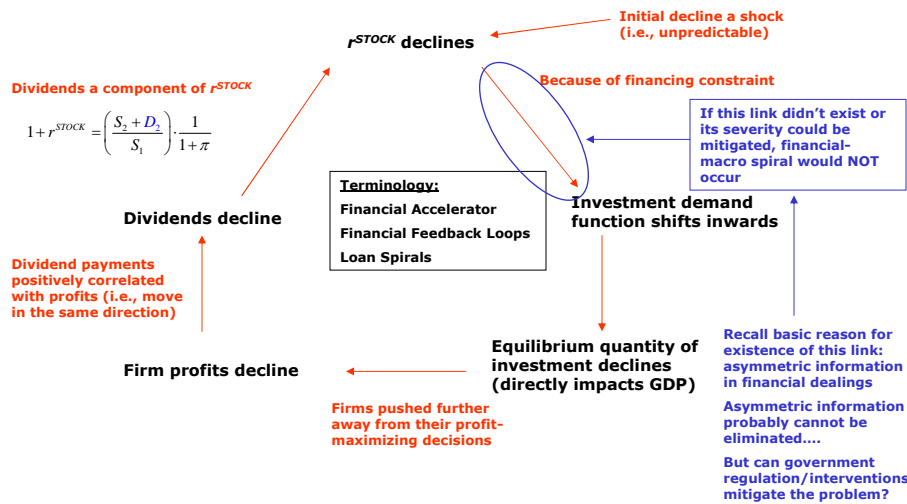
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POLICY AND REGULATORY RESPONSES

- Entire accelerator mechanism due to financing constraint

$$P_1 \cdot (k_2 - k_1) = R \cdot S_1 \cdot a_1$$

- Lagrange multiplier related to asset returns and government regulation by

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Will these programs work as intended?
We'll see...

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REAL INTEREST RATE

- ❑ r a key variable for macroeconomic analysis
- ❑ Chapter 4: r measures the price of period-1 consumption in terms of period-2 consumption
- ❑ Chapter 8: r reflects degree of impatience
- ❑ Midterm Exam (Question 1b): r reflects rate of consumption growth between periods
- ❑ Chapter 6: r measures the price/return of physical assets (i.e., machines and equipment) of firms
 - ❑ "Safe" assets

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- ❑ Now: r also measures price/return of "risky" assets (i.e., stock) in "steady state"
 - ❑ If $r = r^{STOCK}$, financing issues don't affect (very much) macroeconomic outcomes
 - ❑ If r and r^{STOCK} deviate significantly
 - ❑ Financial conditions of firms matter for investment/output
 - ❑ And can matter very importantly!

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